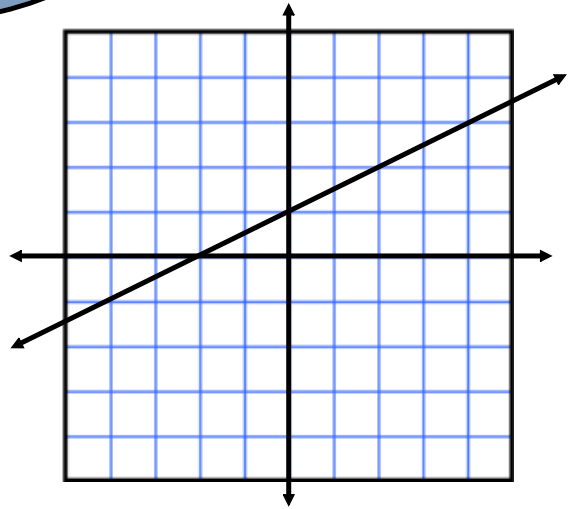


**Calculus AB**  
1-2  
Limits

Examine:  $f(x) = \frac{1}{2}x + 1$

$f(0) =$

$f(2) =$



New Concept:  $\lim_{x \rightarrow 2} f(x) =$

One sided limits:

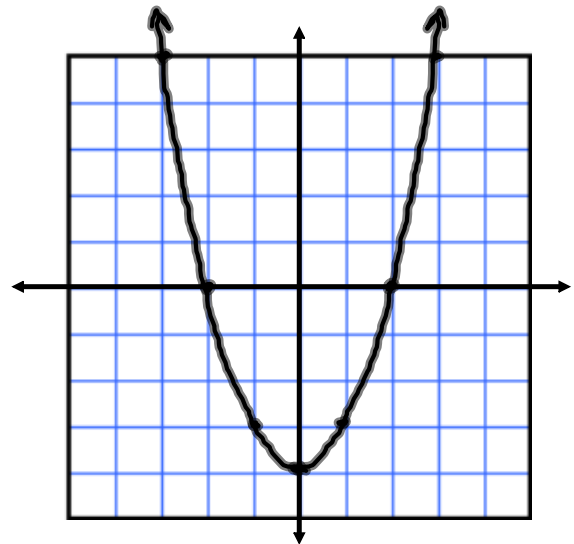
Examine:  $f(x) = x^2 - 4$

Left-hand Limits -

$\lim_{x \rightarrow 1^-} f(x) =$

Right-hand Limits -

$\lim_{x \rightarrow 1^+} f(x) =$



**Theorem - The existence of a limit**

Does  $\lim_{x \rightarrow 1^-} f(x)$  exist? If so, what is it?

How is evaluating a limit different from evaluating a function?

Consider:

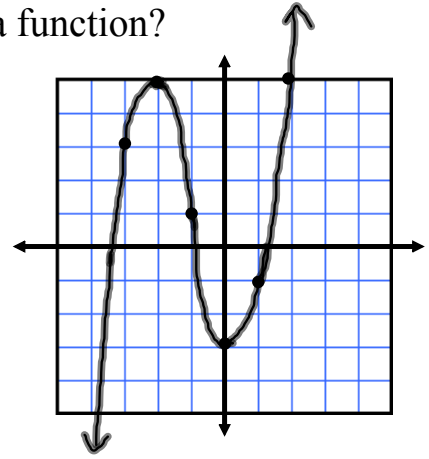
$$f(x) = x^3 + 3x^2 - 2x - 3$$

$$\lim_{x \rightarrow -2^-} f(x) =$$

$$\lim_{x \rightarrow -2^+} f(x) =$$

$$\lim_{x \rightarrow -2} f(x) =$$

$$f(-2) =$$



Using your calculator, graph

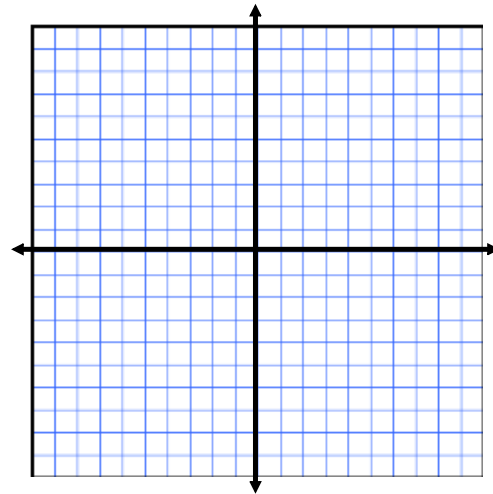
$$f(x) = \frac{x^2 - 5x - 6}{x + 1}$$

$$\lim_{x \rightarrow -1^+} f(x) =$$

$$\lim_{x \rightarrow -1^-} f(x) =$$

$$\lim_{x \rightarrow -1} f(x) =$$

$$f(1) =$$



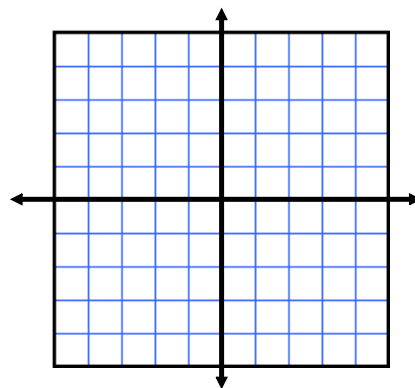
Examine the graph of

$$f(x) = \frac{1}{x}$$

$$\lim_{x \rightarrow 0^-} f(x) =$$

$$\lim_{x \rightarrow 0^+} f(x) =$$

$$\lim_{x \rightarrow 0} f(x) =$$



## Handout 4 - 11 all

(excerpt from the  
Stewart book)